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Algorithm Analysis

By-Subba Reddy sir

- Theory
- Explanation
- Derivation
- Example
- Shortcuts
- Previous Years Question With Solution

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Reference: Introduction to Algorithm By Cormen

Syllabus: (1) Analysis

u (2) Divide and conquer.

y (3) Greedy Technique.

y (4) Dynamic programming.

(5) Hashing & Tree and graph Traversal.

Definition: It is a combination of sequence of finite steps to solve a problem.

Example: Multiplication of Two Numbers

MTN() {
1. Take 2 no's (a, b).
2. Multiply a and b and store result in c.
3. return c
}

from which function we have come, we have to return there.

- finite steps - finite time should be there (But it doesn't mean finite steps always leads to finite time)
- infinite steps - Infinite time
- All steps are compulsory, so combination is required, so finally it can solve the problem.

printf \rightarrow c } syntax
cout \rightarrow c++ }

Properties of Algorithm

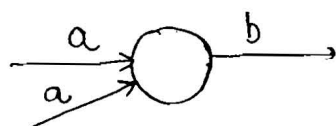
1. It should Terminate after finite time.

2. It should produce "atleast" one output ($M \times n$ output)

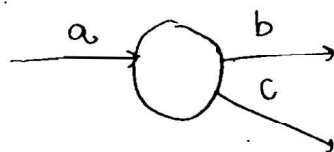
3. It should take "0 or More input"

4. It should be "deterministic."

(different behaviour - Non-deterministic)
deterministic - always same answer.



deterministic (finite steps) also there.

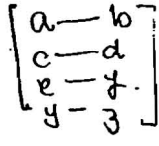


2 O/Ps. Non deterministic.

No dependency \rightarrow so we can swap the steps of Algo.
 Non deterministic \rightarrow special case.

Steps Required to Design Algorithm:

1. Problem definition. (knowing problem clearly).
2. Design Algorithm.
 - divide and conquer
 - greedy technique
 - Dynamic Prog.
 - Backtracking
 - Branch & Bound (BB).



Algorithm Design: After knowing the problem, Map the problem to the existing Algorithm.

3. draw flowchart (Diagramatic Algorithm).
4. Testing and verification. (The Report we made (test cases) ^{our Prog} should Run for those i/ps)
5. coding or implementation.
6. Analysis the Algorithm.
 - Run - MM (go to Run)
 - Base - Hard disk
 - Running time \rightarrow MM (space complexity).
time complexity.

} operating system process state diagram.

Design and Analysis of Algorithm.

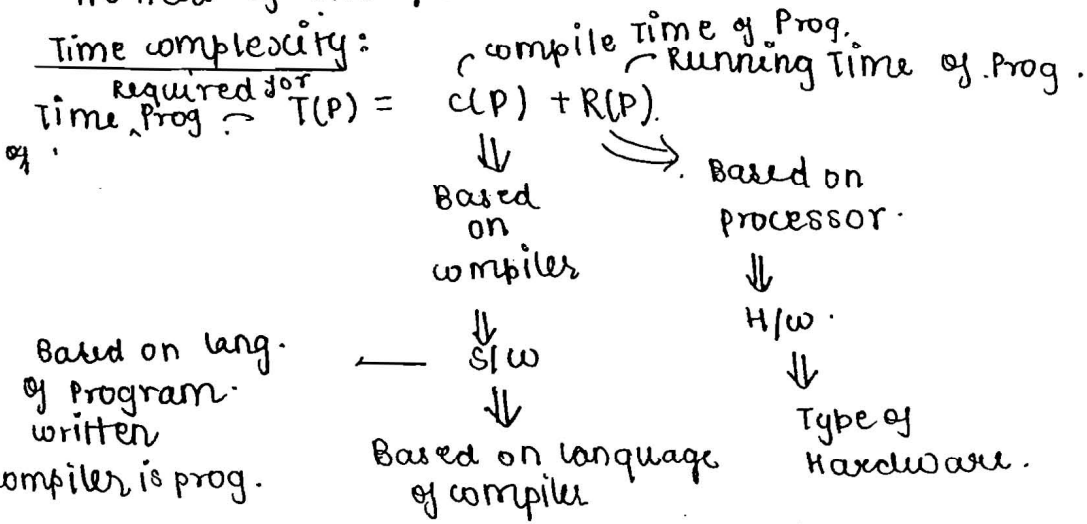
Analysis: chapter 1

If your problem having more than 1 solution, Best one will be decided by analysis based on 2 factors.

1. Time complexity (CPU Time)
2. Main Memory (space complexity).

If your Problem having only 1 solⁿ, go with that solⁿ no need of Analysis.

Time complexity:



Types of Analysis

1. A posteriori Analysis.
2. A priori Analysis

postponing the things.
 (By asking a question, instead of giving answer, asking question to us).

A posteriori.

① It is based on (dependend) on language of compile & Type of H/w.

Adv. ② Exact Answer
 bcoz we are considering Real things).

Dis. ③ system to system different Answer (diffⁿ Time)
 (constants differ sys to sys)

"it is Relative Analysis".

Here processor & compiler lang. is imp.

A priori

① It is independent on lang - c. & type of H/w.

② Approximate Answer

Advantage.

③ system to system. same Answer (same ans. with diffⁿ sys. ans).

"Absolute Analysis".

if prog is running faster prog. written in great logic.

NOTE: Everyone cannot buy supercomputer but every one can write supercomput algo. because lord is given same brain to all. But some people will use it some people will not use it.

software company uses - Apriory Analysis.

APriori Analysis:

we are finding strength of logic.

"It is a determination of order of Magnitude of a statement."

↓
while running statement is running how many times.

ex ①

main()

```
{
1. x = y + z;  => 1 (order of Magnitude).
}
```

put Big Oh (O) before - oqk.
O(1)

ex ②

main()

```
{
  x = y + z; 1
  for (i=1; i ≤ n; i++)
  {
    x = y + z; n.
  }
}
```

n + 1 = O(n)

initializat = 1
condition = n + 1
statement = n.
i++ = n.

exp ③

main()

```
{
  x = y + z; ①
  for (i=1; i ≤ n; i++)
  {
    x = y + z; n
    for (j=1; j ≤ n; j++)
    {
      x = y + z; n.n
    }
  }
}
```

in bracket is 1 statement
is their No bracket.

1 + n(n).
1 + n(n²) = O(n²)

outer loop - add
inner loop = multiply

Time complexity is finding bigger loops.
(where CPU spending more time).

Give this part to cache memory, so CPU got to know that it is spending more time, then program is fast.

Locality of Reference — cache memory; (which is more imp)

Example (4)

```
main()
{ while (i ≤ n)
```

incrementation.

```
{
  i = i + 1
  i = i + 4
  i = i + 5
}
```

$i = i + 10 \Rightarrow \frac{n}{10} \Rightarrow \frac{1}{10} \cdot n$
 $\Rightarrow O(n)$

How many times loop is executing $n/10$.

```
main()
{ i = n
  while (i ≥ 1)
```

decrementation.

```
{
  i = i - 1
  i = i - 9
}
```

$i = i - 10 \Rightarrow \frac{n}{10} \Rightarrow O(n)$

*

```
i = i - 1 > -10
i = i - 9 >
i = i + 7 > 10
i = i + 3 >
```

$i = -10 + 10$
 $i = 0$
not incrementing no decrementing
infinite loop

example: 5

```

main()
{
  i = 1;
  while (i <= n)
  {
    i = 2 * i;
  }
}

```

$1 < 64 \checkmark$
 $2 < 64 \checkmark$
 $4 < 64 \checkmark$
 $8 < 64 \checkmark$
 $16 < 64 \checkmark$
 $32 < 64 \checkmark$
 $64 < 64 \times$

 $64 - 6 \text{ steps}$
 $32 - 5 \text{ steps}$
 $16 - 4 \text{ steps}$
 $n = \log_2 n$

Proof
 1
 3
 3^2
 \vdots
 $3^k = n$
 $\log_3 3^k = \log_3 n$
 $k = \log_3 n$

 $2^k = n$
 $\log_2 2^k = \log_2 n$
 $k = \log_2 n$

$i = 2 * i$
 $i = 3 * i$

 $i = 2 * i * 3$
 $i = 6i$
 $k = \log_6 n$

$i = 2 * i$
 $i = 3 * i$
 $i = 5 * i$
 \Rightarrow
 $i = 30i$
 $O(\log_{30} n)$

II

```

main()
{ while (i >= 1)
  {
    i = i/2  $\Rightarrow O(\log_2 n)$ 
  }
}

```

n
 $n/2$
 $n/2^2$
 $n/2^3$
 \vdots
 $n/2^k = 1$
 $n = 2^k$
 $\log_2 n = k$

$i = i/2$
 $i = i/3$
 $i = i/4$
 $\Rightarrow i/24$
 $\log_{24} n$

main()

if i=10.

i = 1;
while (i ≤ n)

{
i = 2 * i
i = 3 * i
i = i + 3
}

60 → 63 → 13

same
Neglect addition

Example: 6

proof

main()

{
i = 2
while (i ≤ n)

{
i = i²

}

}

main()

{
i = 2
while (i ≤ n)

{
i = i^k

}

}

2
2²
2^{2²}
2^{2^{2²}}

2 < 1000
4 < 1000
16 < 1000
256 < 1000
(256)² < 1000 x

2 = 2^{2¹}
2² = 2^{2²}
(2²)² = 2^{2³}
(2⁴)² = 2^{2⁴}
(2⁸)² = 2¹⁶ ⇒ 2²⁴

{
k

2^{2^k} = n.

2^{k log₂ 2} = log₂ n.

k log₂ 2 log₂ 2 = log₂ (log₂ n)

k = (log₂ (log₂ n))

2^{12¹}
2^{12²}
2^{12³}
2^{12⁴}
⋮
2^{12^k}

log₂ 2^{12^k} = log₂ n

log₁₂ 2^{12^k} = log₁₂ log₂ n.

log₂ log₂ 1000.

2¹ = 2¹ = 2
2² = (2¹)² = 2^{2¹}
2⁴ = (2²)² = (2^{2²})
2⁸ = (2⁴)² = (2^{2³})²

~~log₂ n~~
2^{12^k} = n.

12^k log₂ 2 = log₂ n.

12^k = log₂ n

k log₂ 12 = log₂ log₂ n

i = i²⁹
i = i²
i = i⁸¹

ex $i = 25 \rightarrow$ inner case 25^{29^k}

ex
 $i = 25$
 $i = i^{29}$
 $i = i^2$
 $i = i^7$

$i = i^{29} \Rightarrow O(\log_{29} \log_{25} n)$
 \checkmark outer Base

$(i^{29})^2 = (i^{58})^7 = i^{406}$
 $O(\log_{406} \log_{25} n)$

Example: 7 For square Reverse is "Root" \Rightarrow Here decreasing

main
 $\{$ while $(i > 2)$ } Termination
 $\{$ $i = i^{1/2}$

$n \rightarrow n$
 $n^{1/2} \rightarrow \dots$
 $(n^{1/2})^{1/2}$
 $n^{1/4}$
 $n^{1/8}$
 $n^{1/16}$

$n^{1/2^k} = 2$ Termination

$\frac{1}{2^k} \log_2 n = \log_2 2$
 $\log_2 n = 1 \times 2^k$

$\log_2 \log_2 n = k \log_2 2$
 $\log_2 \log_2 n = k$

$\frac{36}{3} = 108$

$\left\{ \begin{array}{l} i = i^{1/36} \rightarrow O(\log_{36} \log_{29} n) \\ i = i^{1/3} \rightarrow O(\log_{108} \log_{29} n) \\ i = i^2 \end{array} \right.$ Termination
 $O(\log_{54} \log_{29} n)$