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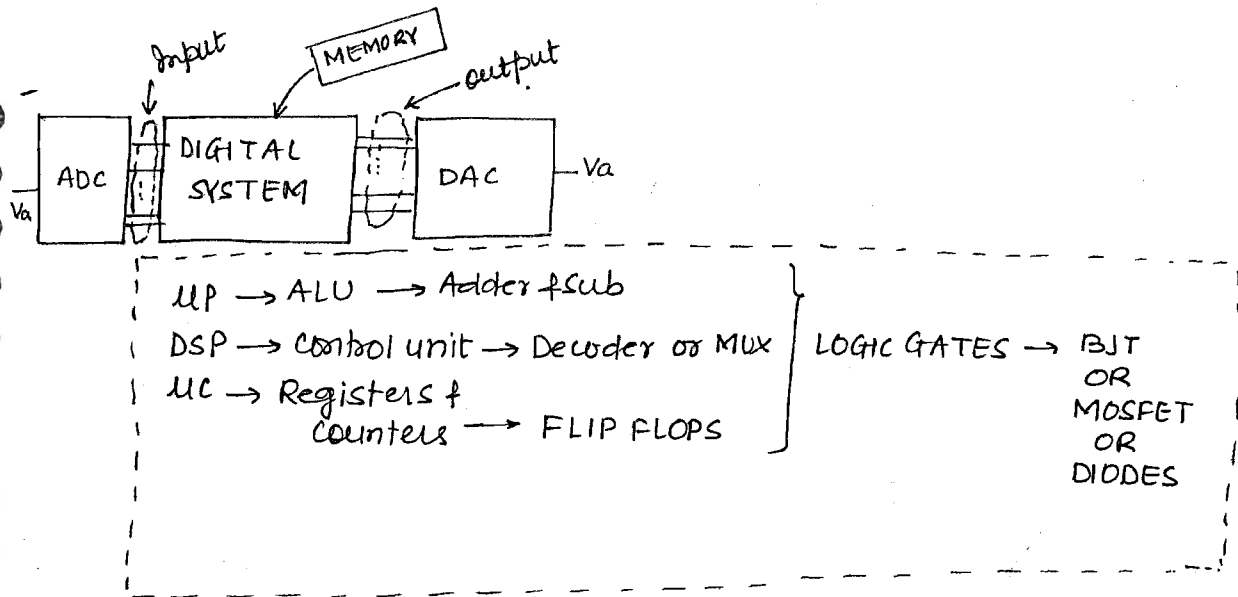
Best Quality Classroom Topper Hand Written Notes to Crack GATE, IES, PSU's & Other Government Competitive/ Entrance Exams

MADE EASY
ELECTRONICS ENGINEERING
Digital Electronics
By- DHANANJAY Sir

- Theory
- Explanation
- Derivation
- Example
- Shortcuts
- Previous Years Question With Solution

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FPGA → Field Programmable Gate Array.

↓
The place where we use the device

SYLLABUS :

I) Basics

- Boolean Algebra.
- Logic Gates.
- K MAP
- Number systems; Codes and Data Representation.

II) Combinational circuits :

i) Arithmetic circuits

- HA, FA, HS, FS
- Parallel Adder
- Look Ahead Carry Adder
- BCD Adder.
- 2's Complement Adder ckt

ii) MULTIPLEXER (Every Gate & IES paper)

iii) DEMUX

iv) DECODER

v) ENCODER

vi) COMPARATOR

vii) CODE CONVERTOR

viii) PARITY GENERATORS/CHECKERS

III) Sequential circuits :

- i) Flip Flops.
- ii) Registers.
- iii) Counters.
- iv) State Machines
 - ↳ Mealy
 - ↳ Moore
 - Newly Added in GATE

iv) ADC's & DAC's.

v) LOGIC FAMILIES :

- i) RTL
 - ii) DCTL
 - iii) IIL
 - iv) DTL
 - v) HTL
 - vi) TTL
 - vii) ECL
- } BJT Based
← Not included in GATE.

- i) NMOS
 - ii) PMOS
 - iii) CMOS
- } FET Based.
(Mainly GATE).

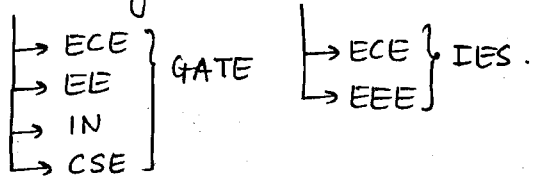
vi) Basics of Semi Conductor Memories.

- i) RAM.
- ii) ROM.
- iii) PAL, PLA
- iv) PROM.

* Preperation Strategy:-

i) class Notes.

ii) Practising Previous Papers.



iii) Reference Books:-

↳ M. Mano

↳ Roth.

↳ Jaub + schilling (ADC + DAC, logic families).

* BOOLEAN ALGEBRA!:

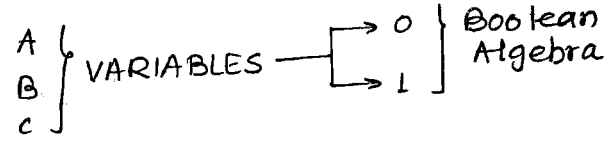
* Introduced in 1854 by GEORGE BOOLE.

* No XOR we available that time, hence designed with help of

i) VENN DIAGRAM

ii) SWITCHES \rightarrow OFF (LOGIC 0)
ON (LOGIC 1)

* Boolean Algebra only handles "0 and 1".



* To minimize logical expressions following methods are used

i) Boolean Algebra (1, 2, 3 variables max^m)

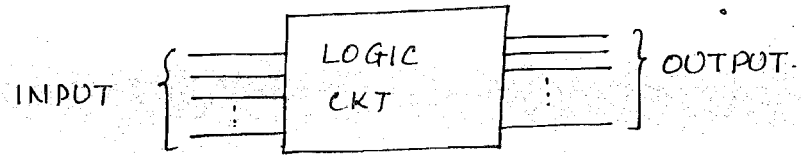
ii) K Map (2, 3, 4, 5 variables at max^m)

iii) Quine Mc'cluskey or TABULATION METHOD (Any no. of variables)

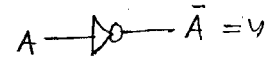
* Boolean Algebra is used when O/P is either "0 or 1"

K Map is used when o/p is either "0, 1 or x"

* THEOREMS IN BOOLEAN ALGEBRA!:



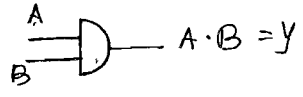
i) NOT!:



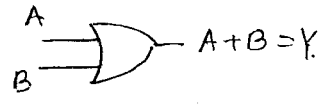
* NOTE!:

$\bar{\bar{A}} = A$ ← NOT operation Relation.

ii) AND!:



iii) OR!:



AND OPERATION

$$\begin{array}{l} 0 \cdot 0 = 0 \\ 0 \cdot 1 = 0 \\ 1 \cdot 0 = 0 \\ 1 \cdot 1 = 1 \end{array}$$

$$\begin{array}{l} A \cdot A = A \\ A \cdot 0 = 0 \\ A \cdot 1 = A \\ A \cdot \bar{A} = 0 \end{array}$$

← AND-OPERATION
THEOREM

OR OPERATION

$$\begin{array}{l} 0 + 0 = 0 \\ 0 + 1 = 1 \\ 1 + 0 = 1 \\ 1 + 1 = 1 \end{array}$$

$$\begin{array}{l} A + 0 = A \\ A + A = A \\ A + 1 = 1 \\ A + \bar{A} = 1 \end{array}$$

OR-OPERATION
THEOREM

Q1) Minimize logic expression:

$$Y = AB + A\bar{B}$$

Soln: $Y = AB + A\bar{B}$

$$Y = A(B + \bar{B})$$

$$\boxed{Y = A}$$

Q2) To implement logical exp; $Y = AB + A\bar{B}C + A\bar{B}\bar{C}$; min^m no. of
2 input NAND Gates

a) 0 b) 1 c) 2 d) 3

Soln: $\boxed{Y = AB + A\bar{B}C + A\bar{B}\bar{C}}$ ← SOP FORM

$$= AB + A\bar{B}(C + \bar{C})$$

$$= AB + A\bar{B}$$

$$= A(B + \bar{B})$$

$$\boxed{Y = A} \leftarrow \text{No Gates Required}$$

Q3) Minimize logic expression; $Y = (A+B)(A+C)$

Soln: $\boxed{Y = (A+B)(A+C)}$ ← POS FORM.

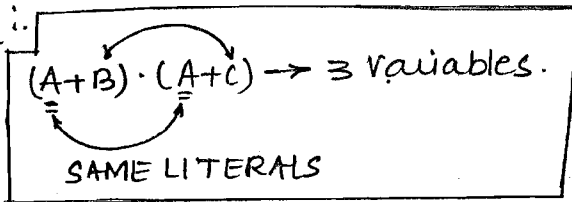
$$Y = A \cdot A + A \cdot C + A \cdot B + B \cdot C$$

$$Y = A + AC + AB + BC$$

$$Y = A(1 + C + B) + BC$$

$$\boxed{Y = A + BC} \leftarrow \text{SOP FORM}$$

Analysis :



$$(A+B)(A+C) = A + BC$$

Q4) Minimize ; $(x+y)(x+\bar{y})(\bar{x}+y)$

$$\begin{aligned} \text{soln: } & (x+y\bar{y})(\bar{x}+y) \\ & = x(\bar{x}+y) \\ & = xy \end{aligned}$$

Q5) Minimize ; $(x+y+z)(x+y+\bar{z})$

$$\begin{aligned} \text{soln: } & (x+y+z)(x+y+\bar{z}) \\ & (x+y)+z \cdot \bar{z} \\ & (x+y) \end{aligned}$$

Note :

$$(A+B)(A+C) = A + BC$$

$$(A+BC) = (A+B)(A+C) \leftarrow \text{DISTRIBUTION THEOREM.}$$

(1+2·3) (1+2) (1+3).

Q8) Minimize ;

- i) $A + \bar{A}B \rightarrow (A + \bar{A})(A+B) = (A+B)$
- ii) $A + \bar{A}\bar{B} \rightarrow (A + \bar{A})(A+\bar{B}) = (A+\bar{B})$
- iii) $\bar{A} + AB \rightarrow (\bar{A} + A)(\bar{A}+B) = (\bar{A}+B)$
- iv) $\bar{A} + A\bar{B} \rightarrow (\bar{A} + A)(\bar{A}+\bar{B}) = (\bar{A}+\bar{B})$

Q9) Minimum no. of Logic gates required for $y = AB + \bar{A}C + A\bar{B}$

$$\begin{aligned} \text{soln: } & y = AB + \bar{A}C + A\bar{B} \\ & = A(B + \bar{B}) + \bar{A}C \\ & = A + \bar{A}C \\ & = (A + \bar{A})(A + C) \\ & \boxed{y = A + C} \end{aligned}$$

Q6) Minimize

$$y = (A+B)(A+\bar{B})(\bar{A}+B)(\bar{A}+\bar{B})$$

$$\begin{aligned} \text{soln: } & (A+B\bar{B})(\bar{A}+B\bar{B}) \\ & A \cdot \bar{A} \\ & = 0. \end{aligned}$$

Q7) Minimize ; $y = A + \bar{A}B$

$$\begin{aligned} \text{soln: } & y = A + \bar{A}B \\ & = (A + \bar{A})(A + B) \\ & \boxed{y = (A + B)} \end{aligned}$$

Note :- The Precedence order of the LOGIC SYMBOLS is :-

$$() > \text{NOT} > \text{AND} > \text{OR} \rightarrow \text{SOP}$$

$$() > \text{NOT} > \text{OR} > \text{AND} \leftarrow \text{POS.}$$

Q10) Minimize ; $y = AB + \bar{A}C + BC$

Soln: $y = AB + \bar{A}C + BC$

Note: 3 variable Available

↳ Repeated twice

↳ Complement on $A + \bar{A}$

$$y = AB + \bar{A}C + BC = AB + \bar{A}C$$

$$(AB + \bar{A}C + BC) = (AB + \bar{A}C) \leftarrow \text{CONSENSUS THEOREM.}$$

Q11) Minimize logical expression:

i) $\bar{A}B + AC + BC = \bar{A}B + AC$

ii) $A\bar{B} + AC + BC = A\bar{B} + BC$

iii) $AB + AC + BC = AC + BC$

← SOP FORM.

POS FORM

iv) $(A+B)(\bar{A}+C)(B+C) = (A+B)(\bar{A}+C)$

v) $(A+B)(A+C)(B+\bar{C}) = (A+C)(B+\bar{C})$

vi) $A\bar{B} + \bar{A}C + \bar{B}C = A\bar{B} + \bar{A}C$

vii) $\bar{A}\bar{B} + \bar{A}\bar{C} + \bar{B}\bar{C} = \bar{A}\bar{B} + \bar{B}\bar{C}$

Note:

*check those literals where $A + \bar{A}$ are present i.e. one literal A is uncomplemented and \bar{A} is complemented.

* Analysis:

$$(A+B)(\bar{A}+C) = A\bar{A} + AC + \bar{A}B + BC = AC + \bar{A}B$$

$$(A+B)(\bar{A}+C) = AC + \bar{A}B \leftarrow \text{TRANSPOSITION THEOREM.}$$

Q12) Minimize ; $y = (A+B)(\bar{A}+\bar{B})$

Soln: $y = (A+B)(\bar{A}+\bar{B})$

$$y = A\bar{B} + \bar{A}B = A \oplus B$$

Q13) Minimize ; $y = (A+\bar{B})(\bar{A}+B)$

Soln: $y = (A+\bar{B})(\bar{A}+B)$

$$y = AB + \bar{A}\bar{B} = A \odot B$$