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By-Prasad sir

- Theory
- Explanation
- Derivation
- Example
- Shortcuts
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COMPILER

Grammar $G = (V, T, P, S)$
variable | Production → start symbol
Terminals

Example → $S \rightarrow ABC$
 $AB \rightarrow CD$
 $C \rightarrow a$
 $D \rightarrow b$

variables: $\{S, A, B, a\}$ → given by grammar (check), otherwise if not given, consider capital letters as variables.

Types of Grammar (according to Chomsky)

1. Type-0 (unrestricted Grammar) — By default, every grammar is Type-0.
2. Type-1 (Context Sensitive Grammar)
3. Type-2 (Context Free Grammar)
4. Type-3 (Regular Grammar)

Type-0 → $\alpha \rightarrow \beta$ — unrestricted because no restrictions
where $\alpha, \beta \in (V+T)^*$

Type-1 → ① Type-0 ($A \rightarrow \epsilon$, production not allowed)
② $|\alpha| \leq |\beta|$

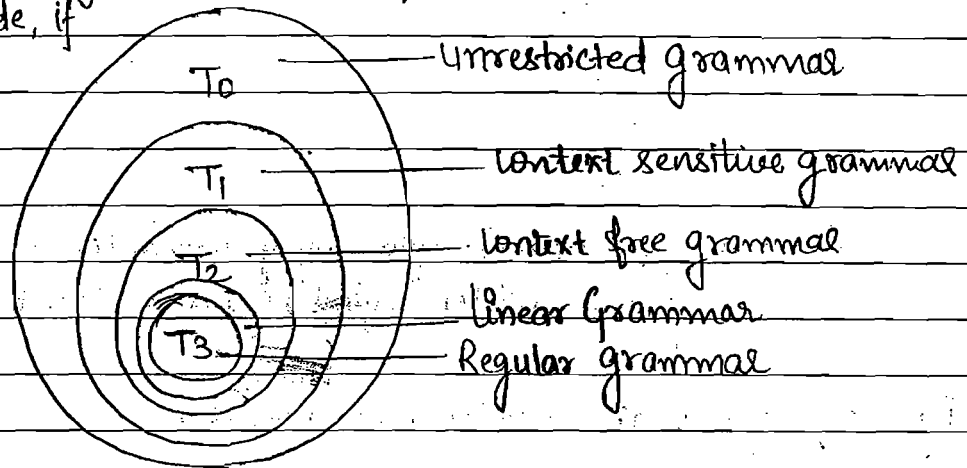
Type-2 → ① $A \rightarrow \beta$ (single variable on left side) no restriction on right side.
② $A \in V$
 $\beta \in (V+T)^*$

Type-3 → ① $A \rightarrow \beta T^* / T^*$ (left linear Grammar)
or $A \rightarrow T^* \beta / T^*$ (Right linear Grammar)

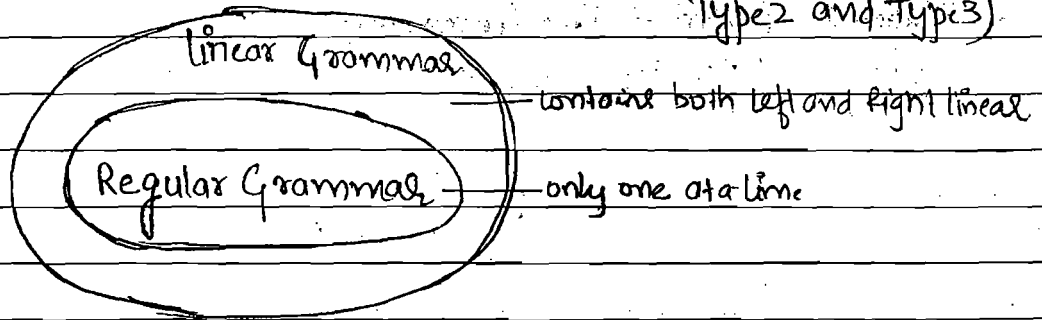
Ex →	S	→ ABC	✓
	A	→ ab	T ₂ , T ₃ (Right side)
	B	→ CD	CFG

① First check left side, single variable, T₂ confirmed

② Then check Right side, if doesn't flow left and right linear, then not T₂(x)



$V \rightarrow T^*VT^*|T^k$ → Linear Grammar (In between Type 2 and Type 3)

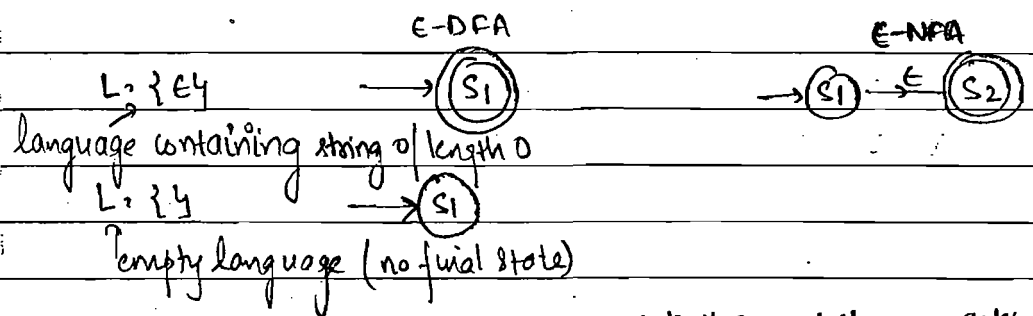


Context Free Grammar (CFG)

① Write a context free Grammar for a language
 $L_2 = \{ a^m b^n \mid m, n \geq 0 \}$

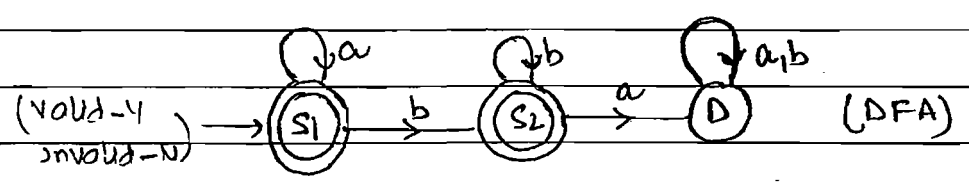
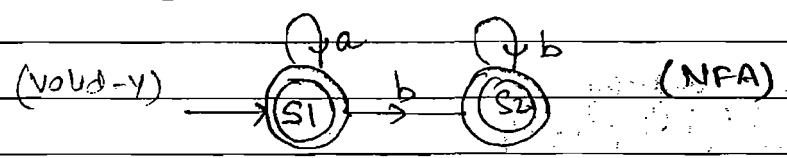
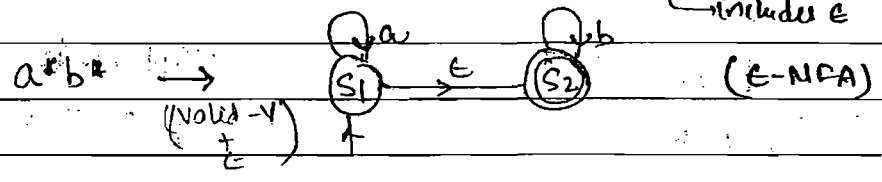
S → AB
 A → aA | ε
 B → bB | ε

ϵ \longrightarrow string of length 0 (empty string)
 $L = \{\epsilon\}$ \longrightarrow Empty language



Transition function \rightarrow any state \times any input \longrightarrow goes to one of state

DFA: $Q \times E \longrightarrow Q$
 NFA: $Q \times E \longrightarrow 2^Q$
 E-NFA: $Q \times E \cup \{\epsilon\} \longrightarrow 2^Q$ (can go to any number of states includes ϵ)



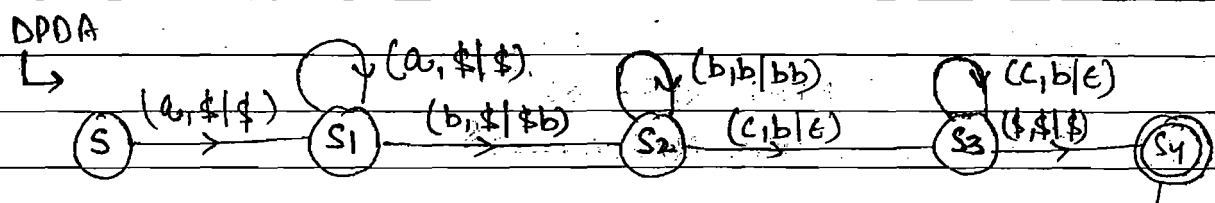
Dead or Trap state \longrightarrow Permanent Non-final states.
 Non-final states \longrightarrow Temporary Non-final states

\longrightarrow Can DFA have more than one final state?
 \hookrightarrow DFA can have multiple final states and dfa doesn't accept the null move (ϵ -X dfa)

② Give context free Grammar for language
 $L = \{ a^m b^n c^n \mid m, n \geq 1 \}$

$S \rightarrow AB$
 $A \rightarrow aA \mid a$
 $B \rightarrow bBC \mid bc$

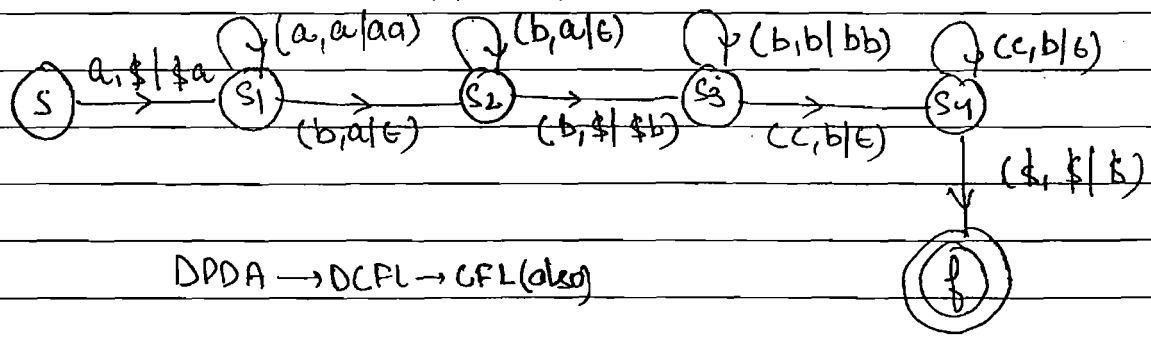
PDA = Finite Automata + Stack



DPDA → acceptance by final state
 → acceptance by empty stack

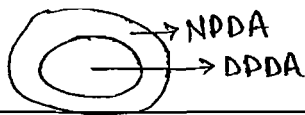
③ Give CFG for the language
 $L = \{ a^i b^{i+j} c^j \mid i, j \geq 1 \}$

$S \rightarrow AB$
 $A \rightarrow aAb \mid ab$
 $B \rightarrow bBc \mid bc$



DPDA → DCFL → CFL (also)

- NFA is equivalent to DFA
- NPDA has more power than DPDA.

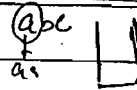


abc



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$$L = \{ a^m b^n c^m \cup a^m b^n c^n \mid m, n \geq 1 \}$$

$$S \rightarrow S_1 / S_2$$

$$S_1 \rightarrow AB$$

$$A \rightarrow aAb / ab$$

$$B \rightarrow cB / c$$

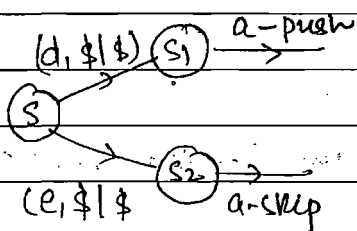
$$S_2 \rightarrow CD$$

$$C \rightarrow aC / a$$

$$D \rightarrow bDc / bc$$

NPDA → CFL language

$$L = \{ damb^n c^n \cup eamb^n c^n \mid m, n \geq 1 \}$$



→ no ambiguity
→ DPDA

⑤ CFG for language $L = \{ a^n b^n c^n \mid n \geq 1 \}$
not CFL → it is CSL

LBA = Finite Automata + 2 stacks

① Union of two DCFL's need not be DCFL.

Px → ④ above. $L = \{ a^m b^n c^m \cup a^m b^n c^n \mid m, n \geq 1 \}$

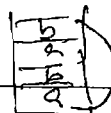
DCFL

DCFL

Union

→ CFL (here in this example)

But can be possible with some example or not.



- ① Intersection of two DCFL's, need not be DCFL.
- ② Intersection of two CFL's, need not be CFL.
- ③ CFL are not closed under complementation.

Ex → $a^n b^m c^n$ complement

↑
CSL

Other than
 $a^n b^m c^n$
Comb

CFL

(Compiler part)

- ④ Given CFG for language $L =$ set of all Arithmetic expressions over the α, β, id .

$E \rightarrow id \mid E + E \mid E * E \mid E - E \mid E / E \mid (E)$

$\alpha \rightarrow +, -, *, /$

$id \rightarrow +, -, *, /$

$\alpha \rightarrow (id + id) \alpha$

$A \alpha \rightarrow id \alpha \mid \beta A$

$\alpha \rightarrow +, -, *, /$

- ⑤ Give CFG for language $L =$ set of all Boolean expressions, over the alphabet 0 and 1.

~~CFG for Boolean expressions~~

$B \rightarrow 0 \mid 1 \mid B \text{ or } B \mid B \text{ and } B \mid \text{not } B \mid (B)$

- ⑥ Give CFG for language $L =$ set of all Regular Expressions over the alphabet a, b ($\epsilon, \{a, b\}$).

$R \rightarrow \epsilon \mid a \mid b \mid R^* \mid R + R \mid R * R \mid (R)$

$(a+b)^*$

$A \rightarrow a \mid b \mid A^* \mid A + A$

$(a+)$

$A + A$

⑦

$a^* b^*$

$R +$

$(R + R)^*$

$(a+b)^n$

- ⑧ Consider the following Grammar

$S \rightarrow aS \mid Sa \mid a$

i/p string: $a^2 a$

How many parse tree?

(Derivation tree)
or
Syntax tree

$a(a+b)^*$

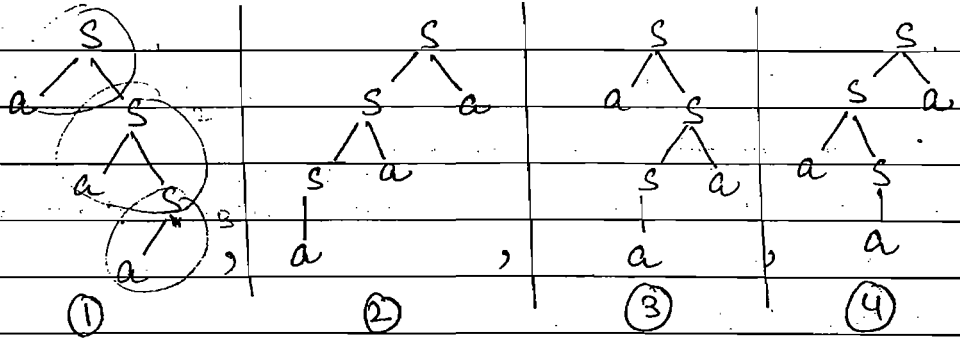
$R \cdot (R + R)^*$

$a \cdot (a+b)^*$

left most derivation \rightarrow always explore 'left most' variable first

right most derivation \rightarrow always explore 'right most' derivation first

string \rightarrow aaa



\rightarrow To know, what string is generated \rightarrow read all leaf nodes from left to right.

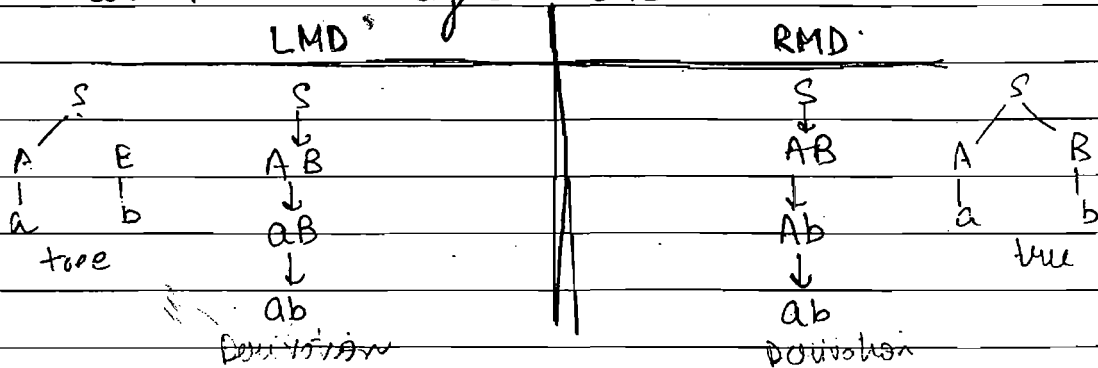
In above, left most derivation tree \rightarrow 4
right most derivation tree \rightarrow 4

even number of too

- ① In above, example, only one variable, so LMDT and RMDT same
- ② if more than one variable, then check (can differ in numbering)
- \rightarrow Always ^{no. of} left Most Derivation tree = no. of Right Most Derivation tree, only numbers changes (which may not even change sometimes)

No. of Left Most Derivation tree = No. of Right Most Derivation tree
= No. of Parse tree

\rightarrow left most Derivation and Right most Derivation may differ, but their trees will always be same.



\rightarrow so, Derivation are differing, but both have same parse tree.

→ Above Grammar is Ambiguous Grammar, because more than one parse tree possible.

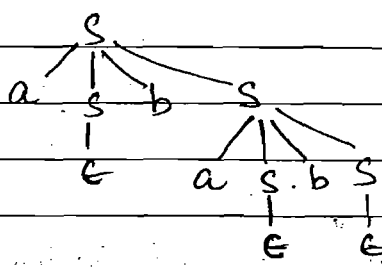
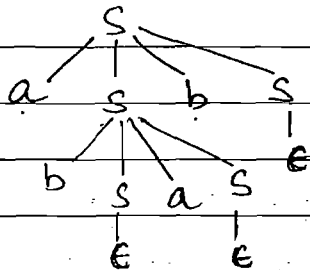
→ A Grammar G is said to be ambiguous, if for atleast one string, more than one parse tree possible

→ Checking given grammar is ~~ambiguous or not~~ ^{undecidable}, because there is no algorithm ambiguous or not, is undecidable, becoz there is no algorithm to check it.

Q) Consider the following grammar

$$S \rightarrow asbs \mid bSas \mid \epsilon$$

input string $\rightarrow abab\epsilon$

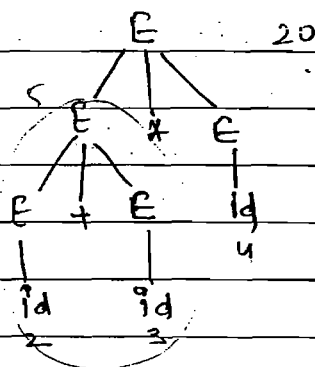
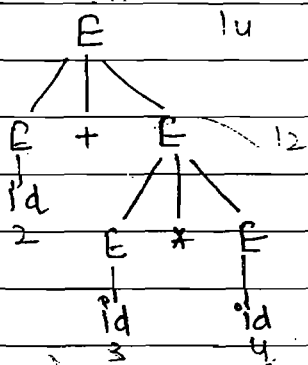


Above is Ambiguous grammar.

Q) Consider the following grammar

$$E \rightarrow id \mid E + E \mid (E * E$$

Input string: $id + id * id$
 $2 + 3 * 4$



→ Ambiguous Grammar.